

# Handbook of Product Graphs, Second Edition

## Errors, Misprints and Notes

December 27, 2014

### Errors, misprints, missing references

- Page 246, Proposition 20.8: The proposition holds for  $\tau^*$ , but not for  $\tau$ .
- Page 258, line 5: replace “Slutzky” with “Slutzki”.
- Page 305, line 16: replace “ $\gamma(G \square H) = \gamma(G)\gamma(H)$ ” with “ $\gamma(G \square H) \geq \gamma(G)\gamma(H)$ ”.
- Page 335, line above Lemma 26.38: replace “ $G \rightarrow \mathcal{C}_n(G)$ ” with “ $H \rightarrow \mathcal{C}_n(G)$ ”.
- Page 336, line above Lemma 26.40: replace “restriction every” with “restriction to every”.
- Page 336, line -5: replace “but  $\chi(\mathcal{C}_3(G)) \geq 3$ ” with “but  $\chi(\mathcal{C}_3(G)) > 3$ ”.
- Page 357, last line: the following paper should be added to the list: J. Žerovnik, Perfect codes in direct products of cycles—a complete characterization, *Adv. in Appl. Math.*, 41 (2008), 197–205.
- Page 385, line 17: replace twice “ $C_m \times C_n$ ” with “ $C_m \times P_n$ ”.
- Page 416, line -12: should read:  $S(\times_{\iota \in I} G_\iota) = \square_{\iota \in I} S(G_\iota)$ ,
- Page 437, line -12: replace “The relationship between the Laplacian of a product and that of the factors is the same as for the adjacency matrix.” by “The relationship between the Laplacian spectrum of a product and that of the factors is very difficult except for the Cartesian product, unless the graphs are regular.”

### Notes

- Chapter 2, Independence number  
Simon Špacapan<sup>1</sup> extended the No-Homomorphism Lemma 2.13 and Theorem 27.13 on the independence number of direct powers of vertex transitive graphs to assertions about the  $k$ -independence number. Notice that

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<sup>1</sup>Simon Špacapan, The  $k$ -independence number of direct products of graphs and Hedetniemi’s conjecture, *European Journal of Combinatorics*, 32 (2011), 1377-1383

the  $k$ -independence number  $\alpha_k(G)$  of a graph  $G$  is the size of the largest  $k$ -colorable induced subgraph of  $G$ .

Both the No-Homomorphisms Lemma and Theorem 27.13 hold if  $\alpha(G)$  is replaced by  $\alpha_k(G)$ .

- Chapter 31.2, Free product

It may seem surprising, but the free product  $G*H$  of graphs is an isometric subgraph of the weak Cartesian product of infinitely many copies of  $G$  and  $H$  (Aleksandra Jędrzejaszek, Free Products of Graphs, Master Thesis, AGH Cracow, 2011).